

Texture Synthesis from Samples for Point-Sampled Geometry*

点模型上基于样图的纹理合成

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Abstract:【Objective】In this paper, we proposed a fast-speed and effective algorithm to synthesize texture over three-dimensional point set surface without triangulation. **【Methods】**At first, the neighborhoods for every point on three-dimensional point set surface were built through KD-tree. Then the local neighborhood construction was obtained and the most matching point was found in the input sample image for every point. Finally, texture synthesis was finished through point-based rendering. **【Results】**The experimental results show that our algorithm can generate continuous and smooth texture on the 3D point-sampled geometry, and maintain the texture structure of the original image. **【Conclusion】**The technique of texture synthesis is effective. Compared with traditional 3D texture synthesis algorithm, this algorithm is less time-consuming, more flexible and controllable.

Key words: texture synthesis, point set surface, sample image, mapping, assignment

摘要:【目的】目前已有的在三维点模型上的纹理合成方法,是将点模型进行三角面片化后再进行纹理合成操作,本研究的目的是避免三角面化的过程,得到一种直接在点模型上操作的、快速有效的纹理合成方法。**【方法】**首先,用KD树为三维点模型上的每一点建立邻域,然后为每一点在样图中寻找最匹配的纹理值,最后通过基于点的绘制技术完成纹理合成。**【结果】**本研究方法能在三维点模型上生成连续光滑的纹理,且保持了原样图的纹理结构。**【结论】**本研究的纹理合成方法是有效的,并且和传统的三维纹理合成算法相比,本方法费时更少、更灵活可控。

关键词:纹理合成 点模型 样图 映射 赋值

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0 Introduction

Texture synthesis from samples (TSFS) has developed rapidly in recent years. The basic thought of TSFS is giving a small piece of sample image to generate large and continuous texture similar to the sample^[1]. TSFS is divided into two-dimensional tex-

ture synthesis from samples (2D-TSFS) and three-dimensional texture synthesis from samples (3D-TSFS). Most of the 2D-TSFS methods regarded generation of texture as a Markov process^[2-3]. These methods worked well but the speeds were very slow. They were improved by the algorithms of the vector coding on texture^[4] and the pyramid synthesis^[5]. The 3D-TSFS methods synthesized the texture over the three-dimensional (3D) geometric surface from samples directly^[6-10]. Based on a given texture sample, the methods generated texture over the entire surface in accordance with the geometric configuration of the surface. The results were visually similar and continuous.

By far, a number of 3D-TSFS techniques have been put forward and most of them were built on grid models. In the texture synthesis algorithms, these traditional techniques used topology information contained in surfaces. There were few researches about synthesizing texture directly on the 3D point set surface.

Recently, point based representations have been proposed as an alternative to triangles for 3D surfaces, with a number of advantages. No ‘mesh’, or connectivity information has to be stored explicitly. This allows a simple and compact representation, ideal for fast rendering and editing.

The original sampling points obtained from the scanner surface are called geometric information. The grid topology information is actually from the original geometric information via complicated processing such as generating triangular patches on point model and so on. In this article, we will synthesize texture directly on 3D point set surfaces without reconstructing grid model from the surfaces which is illustrated in figure 1.

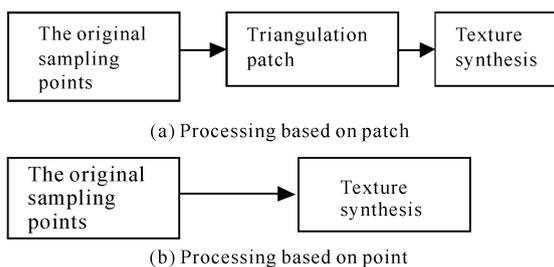


Fig. 1 Comparison of the two processing procedure

1 Related work

A large number of algorithms of texture synthesis from samples have been proposed. Heeger and Bergen^[11] synthesized texture using the Laplace and controllable Pyramid. Debonet used a similar approach. Efros and Leung brought forward a more direct algorithm. Firstly they set a few seeds in the surface to be synthesized and then found the matching points in the sample via the given neighborhood, and finally randomly selected a match point to complete the rendering^[12]. Wei and Levoy^[4] proposed a similar algorithm and greatly accelerated the process of synthesis by means of vector quantization. Efros^[8] brought out a texture synthesis algorithm based on block collage. In the meantime, Wei^[10] used a multi-scale algorithm to synthesize surface texture. Turk^[13] used a similar approach. Zhang^[14] proposed the gradient texture method which obtained gradient texture effect on the surface. BTF’ synthesis method generated a wealth of micro-structure on the surface^[15]. While most of these methods were based on triangle mesh, there were few of them could achieve the synthesis closing to interactive rate^[8]. The methods of texture synthesis could be extended to the processing of the other things. For example, we could generate voice^[16], sport^[14] and video^[17-18] via texture synthesis. Moreover, the techniques of texture synthesis could be used to repair image and video.

Abandoning triangulation methods, the image processing technologies on point-based surfaces only record the information of points, from which the final image can be reconstructed. The technologies provide new avenues for solving fast image processing of a large number of three-dimensional sampled points data. In the last few years, a large number of papers related to point-based surfaces have emerged. We briefly outline those related to our work. Clarenz and Rumpf^[19] researched how to do the geometry processing of finite elements on point based surfaces and proposed a pixel-based algorithm to synthesize surface texture as an example. Xiao and Zhao^[20] presented a novel technique for texture synthesis on point-sampled geometry using global

optimization. By adding special extra terms to the energy function, the authors implemented a user controllable texture synthesis algorithm for point set surfaces on 3D flow fields. The experimental results have greatly increased.

2 The Process of Texture Synthesis

We propose a high speed and effective algorithm to synthesize the texture over 3D point set surface abandoning triangulation. The flow chart of texture synthesis on 3D point set surface is illustrated in figure 2 and the basic steps can be summarized as follows.

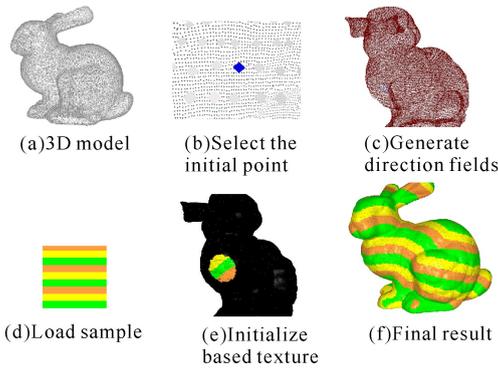


Fig. 2 Flow chart of texture synthesis on 3D point set surface

2.1 Establishing the neighborhood relationship of the points on the 3D model

We select an initial point or more on 3D point set surface in the first step and load the data of sample pattern to obtain texture data of pixels point in the sample.

The points distributing on the 3D point model are discrete, so we need to establish the relationship among the points to prepare for the texture synthesis. In our algorithm, we establish neighborhood relations of the points via KD-tree, so each of the points on the 3D surface has a set of adjacent points as its neighborhood points. The size of the neighborhood can be adjusted by the parameters of KD-tree, so we can acquire suitable neighborhood relations.

2.2 Initializing texture values

Initialization is indispensable in the process of the texture synthesis. The initial texture value on the 3D surface is acquired via initializing the texture of the initial point which we obtain in the first step, and it is regarded as the based texture for texture

synthesis. But it is not enough if we only synthesize the initial point. To solve this problem we put the neighborhood points of the initial point into the ranks of initialization, and their texture values are also regarded as the based texture. Initializing texture is divided into three steps:

1) Assign the initial point i a texture value from the sample image randomly.

2) Calculate the texture values of the neighborhood points of i .

a) Projecting the direction between i and all surrounding points i_k onto i 's tangent plane and retaining the distance information.

Projecting:

$$\text{Direction}[i_k] = \text{points}[i_k] - \text{pos-points}[i]$$

$$\text{Direction}[i_k] = \text{Direction}[i_k] -$$

$$\text{Dot}(\text{Direction}[i_k], \text{normal}[i]) * \text{normal}[i]$$

Normalizing:

$$\text{Direction}[i_k] = \text{Normalize}(\text{Direction}[i_k])$$

Calculating the distance between i_k and i :

$$d = \text{Euclid_diance}(i_k, i)$$

Retaining the distance information:

$$\text{Direction}[i_k] = d * \text{Direction}[i_k]$$

b) The direction of i is recorded as d and the normal vector of i is recorded as n . We create a new coordinate system on i 's tangent plane. The point i is the origin of coordinate. The direction d is Y -axis. The direction $n \times d$ is X -axis ($n \times d$ is derived from the vector cross product formula of solid geometry).

Regarding the average distance h between points and points on 3D model as a unit, we calculate the step length $\Delta x, \Delta y$ on X -axis and Y -axis for each projection vector obtained in the previous step.

c) In the sample image, regarding the point which a texture value has been assigned to the initial point as the center and pixel as the unit, we find the point whose distance to the center is $\Delta x, \Delta y$ units respectively on X -axis and Y -axis and assign the texture value of the point to the neighborhood point corresponding with the point projection vector. For each neighborhood point, the operation is repeated.

3) Initialize the border set

All of the points on 3D model are divided into three sets of points Y, B, N . The points having tex-

ture value belong to the set Y . The points without a texture value and near to the points of Y belong to the set B —The border set. The other points belong to the set N .

Attach a label to the points with initialized texture value and put them into set Y . The distances between each point in the set Y and the initial point i are calculated and saved to the variable geodesic_distance $[i_k]$.

Attach a label to the neighborhood points i_{kn} of the points in the set Y and without a texture value, and put them to the border set B . The distances between each point in the set B and the initial point i are calculated via the following formula:

$$\text{geodesic_distance}[i_{kn}] = \min \{ \text{geodesic_distance}[i_k], \text{geodesic_distance}[i_k] + \text{Euclid_distance}(i_k, i_{kn}) \}.$$

2.3 Establishing orientation field over 3D surface

We must specify directions on 3D point set surface before texture synthesis, because sample texture has directivity. The directions of a few points can be specified by the user and the directions of the absolutely major points have to acquire directions via algorithm. The algorithm used the method similar to Dijkstra's. The geodesic distances between the user-specified point and the other points were calculated. The new direction was calculated as the sum of the directions of all adjacent points having directions, weighted using the Gaussians. The direction of each point was acquired from the near to the distance. So the orientation field over the surface was established.

2.4 Selecting the next point

Selecting the next point to be rendered is the first step in the core of texture synthesis. We need to select the point matching the condition as the next point. If we select the next point from all of the points on the point based model, the speed of texture synthesis will be very slow. To solve this problem we use the border set B .

Selecting the next point from the border set B can greatly narrow the scope of the operation and improve the efficiency of texture synthesis. Every point in the set Y and B contains information about

the distance to the closest point with a texture value. The point with the smallest distance from B is selected as the next point p .

2.5 Establishing the mapping between the next point and the sample image

In order to calculate the texture value of the point p and finish rendering, the mapping between the point p and the sample is established, and then the best matching texture value in the sample is found out.

The process to establish mapping between the point p and the sample is as follows:

1) Projecting the direction between p and all surrounding points onto p 's tangent plane and retaining the distance information (Similar to our method used in section III.2.1).

2) Creating a new coordinate system and establishing a regular matching grid in the coordinate system.

The direction of p is recorded as d and the normal vector of p is recorded as n . We create a new coordinate system on p 's tangent plane. The point p is the origin of coordinate. The direction d is Y -axis. The direction $n \times d$ is X -axis (Similar to our method used in section III.3.1).

With the point p as the center, we build a $N \times N$ grid G of $N \times N$ points t_{ij} with a distance of h in the new coordinate system. The numerical value h is the average distance between points and points on the 3D model. In this article we establish the mapping between the points on the 3D model and the pixels in the sample via the grid G .

3) Assigning the texture value to the points t_{ij}

For each point t_{ij} on the grid G , we select the closest projected point p_{ij} . On the 3D point set surface we find out the point m_{ij} corresponding to p_{ij} . If the point m_{ij} belongs to the set Y , we assign the color of m_{ij} to t_{ij} and t_{ij} is marked as assigned. Else, t_{ij} is marked as unassigned.

2.6 Finding the value of texture and assignment

In the sample, with each of the points as the center and pixel as the unit, we build $N \times N$ grids from which we find out the grid C with minimum color difference via comparing all grids to the grid G as illustrating in figure 3. The color of the center

point q of grid C is the texture value of the point p .

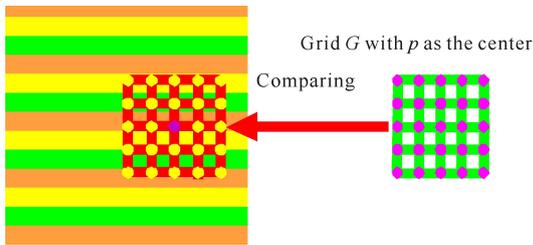


Fig. 3 Searching the matching point in the sample

In this article, we propose a new assignment method. As well as following the traditional pattern of single-point assignment, we carry out a new algorithm for multi-point synchronous assignment via the neighborhood and mapping relations. The new assignment method is divided into two steps:

1) Single-point assignment for the point p

We assign the color of the center point q of grid C to the point p . The point p is marked as assigned and included in the set Y . We attach a label to the p 's neighborhood points without the texture value, and put them to the border set B .

2) Multi-point synchronous assignment

We find out the points t_{ij} of the grid G that have not the texture value and the points m_{ij} of the 3D model corresponding with them. We assign the color of the corresponding points of grid C to the points m_{ij} and finish assignment. The points m_{ij} are marked as assigned and included in the set Y . We attach a label to the m_{ij} 's neighborhood points without the texture value, and put them to the border set B .

2.7 Assignment and rendering

We repeat the processing in section III. 2. 4 ~ 2. 6 until each point on the 3D point set model has a texture value and is rendered.

3 Results

We carry out our algorithm on the computer with processor 1 600 MHz and core storage 256 MB. We synthesize texture on 3D bunny model with 35 283 sampling points. On the model, the average distance h between points and points is 0. 012 528. In the experiment, we obtain different results via changing parameters. The results are presented in table 1 and figure 4.

Table 1 The experiment data of texture synthesis on 3D point set surface

Size of sample	Size of grid	Size of KD-tree (points)	The time of initialization (s)	The time of texture synthesis (s)
64×64	11×11	300	0. 000 7	35
64×64	21×21	600	0. 001 1	37
88×76	21×21	600	0. 000 7	70
100×100	21×21	600	0. 033 0	115
128×128	21×21	600	0. 000 8	208



Fig. 4 Results of texture

4 Conclusions

We have presented a fast-speed and effective algorithm to synthesize texture over 3D point set surface abandoning triangulation. We finish texture synthesis via seven steps. The experimental results show that the method can produce smooth texture synthesis as well as keeping the structures in the sample texture and the speed of processing is fast. In the future, we will further enhance the effect and the speed of texture synthesis on piont set surface. Moreover, we will reseach texture synthesis on piont set surface from Multi-sample images.

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